

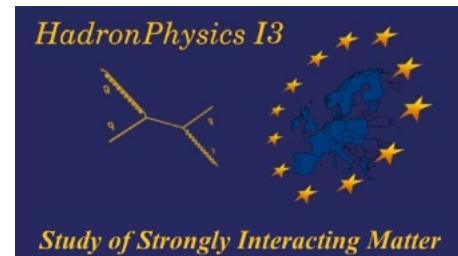
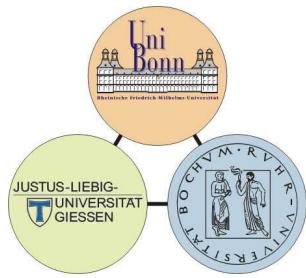


The pion cloud of the nucleon: Facts and popular fantasies

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CONTENTS

- Introductory remarks & disclaimer
- Dispersion relations: Theoretical framework
- Discussion of the spectral functions
- Results for space- and time-like ffs
 & the pion cloud
- Summary and outlook

with: Maxim A. Belushkin, Hans-Werner Hammer

Introduction

REMARKS & DISCLAIMER

- Analyze nucleon em ffs using dispersion theory w/ input from chiral perturbation theory, draw conclusions about the pion cloud
 - What can we say (*or not*) about the pion cloud of the nucleon?
 - ★ concept originated soon after Yukawas proposal of the pion
Heisenberg, Wentzel, Pauli, Kemmer, ...
 - ★ in general, not a well-defined concept → requires some modelling
 - ★ pion cloud = pion loops in CHPT?
yes, but this clearly shows the limitations of the concept
In general, any observable receives contributions from pion loops and short-distance operators → reshuffling since only **physical observables** are RG invariant
- $\frac{d}{d\lambda} \mathcal{O}(\lambda) = 0$
- ⇒ let us analyze this in more detail

LOOPS vs CONTACT OPERATORS: AN EXAMPLE

Bernard, Hemmert, M., Nucl. Phys. A **732** (2004) 149 [hep-ph/0307115]

- the isovector Dirac radius of the proton at third order in the chiral expansion

$$\langle r^2 \rangle_1^V = \left(0.61 - (0.47 \text{ GeV}^{-2}) \tilde{d}(\lambda) + 0.47 \log \frac{\lambda}{1 \text{ GeV}} \right) \text{ fm}^2$$

- dimension-3 LEC \tilde{d} parameterizes the nucleon “core”
- pion loops give const + chiral logarithm (at fixed pion mass)
- empirical value for pairs of $(\lambda[\text{GeV}], \tilde{d}(\lambda)[\text{GeV}^{-2}])$, e.g.

$$(1.0, +0.06) , \quad (0.943, 0.0) , \quad (0.6, -0.46)$$

- ⇒ the “core” contribution is only positive for $\lambda > 943 \text{ MeV}$
- ⇒ at odds with naive expectations

- this is an extreme case, but it nicely illustrates the point

WHY DISPERSION RELATIONS for the NUCLEON FFs ?

- Model-independent approach → important non-perturbative tool to analyze data
- Dispersion relations are based on fundamental principles: **unitarity & analyticity**
- Connect data from small to large momentum transfer
as well as time- and space-like data
- Allow for a **simultaneous analysis** of all four em form factors
- Spectral functions encode perturbative and non-perturbative physics
e.g. vector meson couplings, multi-meson continua, **pion cloud**, ...
- Spectral functions also encode information on the strangeness vector current
→ sea-quark dynamics, strange matrix elements
- Allow to extract nucleon electric and magnetic radii
- Can be matched to chiral perturbation theory

Theoretical framework

BASIC DEFINITIONS

- Nucleon matrix elements of the em vector current J_μ^I

$$\langle N(p') | \mathbf{J}_\mu^I | N(p) \rangle = \bar{u}(p') \left[\mathbf{F}_1^I(t) \gamma_\mu + i \frac{\mathbf{F}_2^I(t)}{2m} \sigma_{\mu\nu} q^\nu \right] u(p)$$

- ★ isospin $I = S, V$ (isoScalar, isoVector)
- ★ four-momentum transfer $t \equiv q^2 = (p' - p)^2 \equiv -Q^2$
- ★ F_1 = Dirac form factor, F_2 = Pauli form factor
- ★ Normalizations: $F_1^V(0) = F_1^S(0) = 1/2$, $F_2^{S,V}(0) = (\kappa_p \pm \kappa_n)/2$
- ★ Sachs form factors: $G_E = F_1 + \frac{t}{4m^2} F_2$, $G_M = F_1 + F_2$
- ★ Nucleon radii: $F(t) = F(0) [1 + t \langle \mathbf{r}^2 \rangle / 6 + \dots]$ [except for the neutron charge ff]

DISPERSION RELATIONS

Federbush, Goldberger, Treiman, Drell, Zachariasen, Frazer, Fulco, Höhler, . . .

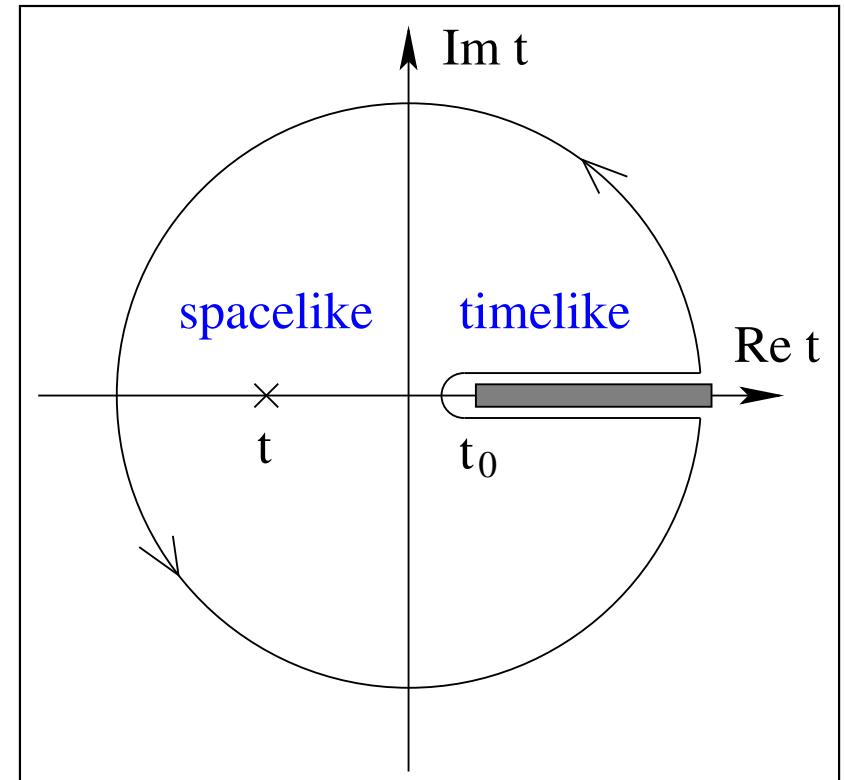
- The form factors have cuts in the interval $[t_n, \infty[$ ($n = 0, 1, 2, \dots$) and also poles
- \Rightarrow Dispersion relations for $F_i(t)$ ($i = 1, 2$):

$$F_i(t) = \frac{1}{\pi} \int_{t_0}^{\infty} dt' \frac{\text{Im } F_i(t')}{t' - t}$$

- no subtractions
[only proven in perturbation theory]
- suppression of higher mass states
- central objects: spectral functions

$\text{Im } F_i(t)$

- cuts $\stackrel{\wedge}{=}$ multi-meson continua
- poles $\stackrel{\wedge}{=}$ vector mesons

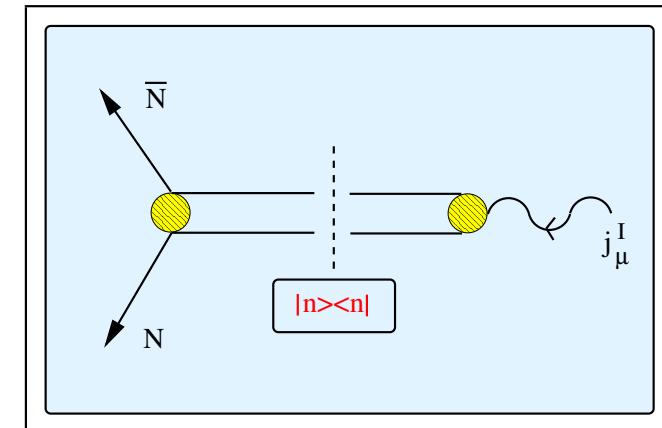


SPECTRAL FUNCTIONS – GENERALITIES

- Spectral decomposition:

$$\text{Im} \langle \bar{N}(p') N(p) | J_\mu^I | 0 \rangle \sim \sum_n \langle \bar{N}(p') N(p) | n \rangle \langle n | J_\mu^I | 0 \rangle \Rightarrow \text{Im } F$$

- * on-shell intermediate states
- * generates imaginary part
- * accessible physical states



- *Isoscalar* intermediate states: $3\pi, 5\pi, \dots, K\bar{K}, K\bar{K}\pi, \pi\rho, \dots +$ poles
 $\rightarrow t_0 = 9M_\pi^2$
- *Isovector* intermediate states: $2\pi, 4\pi, \dots +$ poles
 $\rightarrow t_0 = 4M_\pi^2$
- Note that some poles are generated from the appropriate continua

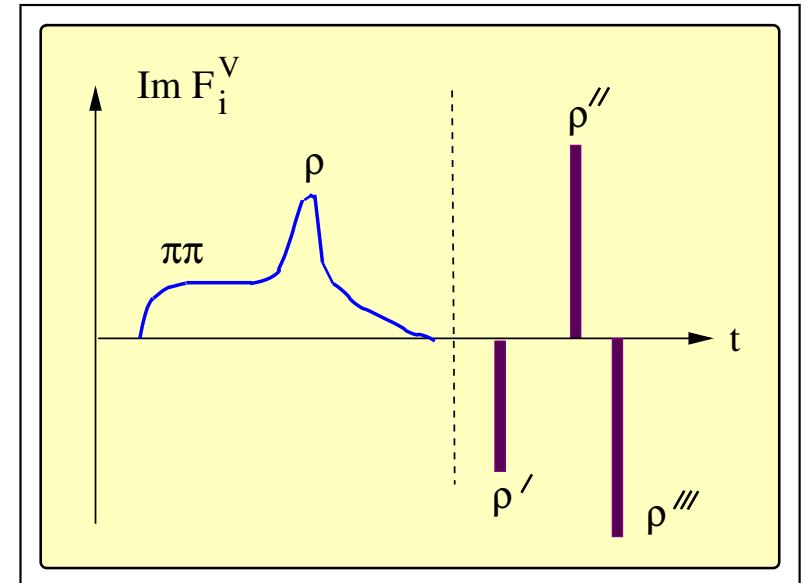
ISOVECTOR SPECTRAL FUNCTIONS

Frazer, Fulco, Höhler, Pietarinen, ...

- exact 2π continuum is known from threshold $t_0 = 4M_\pi^2$ to $t \simeq 40 M_\pi^2$

$$\text{Im } F_i^V(t) = \frac{q_t^3}{\sqrt{t}} |F_\pi(t)|^2 J_i(t)$$

- * $F_\pi(t)$ = pion vector form factor
- * $J_i \sim$ P-wave pion-nucleon partial waves in the t-channel



- Spectral functions inherit singularity on the second Riemann sheet in $\pi N \rightarrow \pi N$

$$t_c = 4M_\pi^2 - M_\pi^4/m^2 \simeq 3.98 M_\pi^2 \rightarrow \text{strong shoulder} \rightarrow \text{isovector radii}$$

- This singularity can also be analyzed in CHPT

Bernard, Kaiser, M, Nucl. Phys. A 611 (1996) 429

- Higher mass states represented by poles (with a finite width)
 - not necessarily physical masses

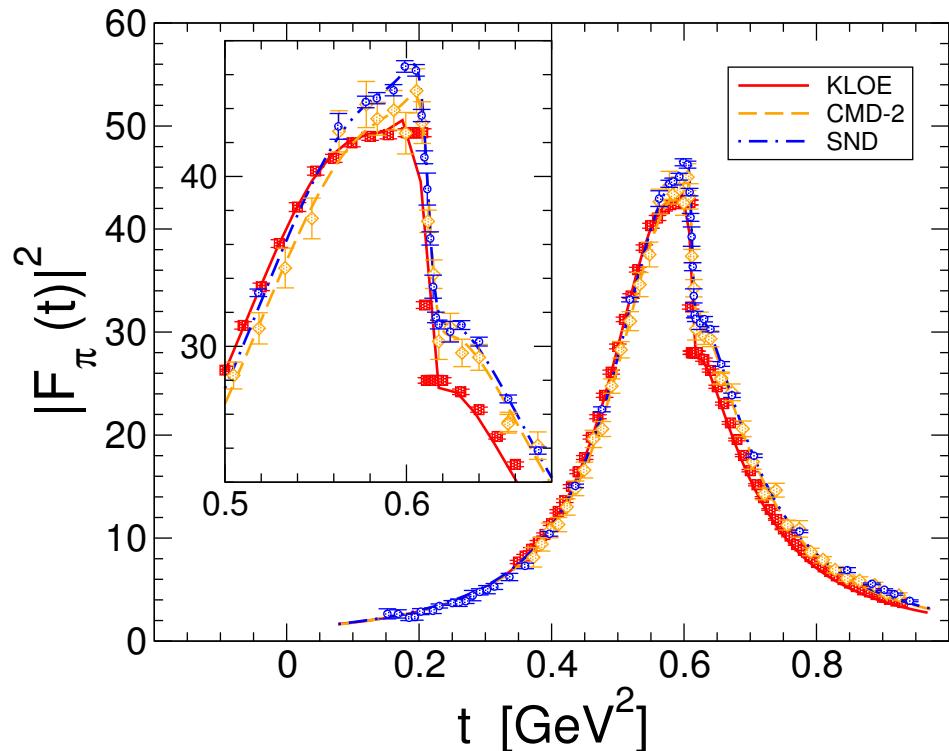
For related work, see Dubnicka et al., J.Phys. G 29 (2003) 405

NEW DETERMINATION OF THE 2π CONTINUUM

12

Belushkin, Hammer, M., Phys. Lett. B 633 (2006) 507 [arXiv:hep-ph/0510382].

- Pion FF from KLOE/CMD-2/SND



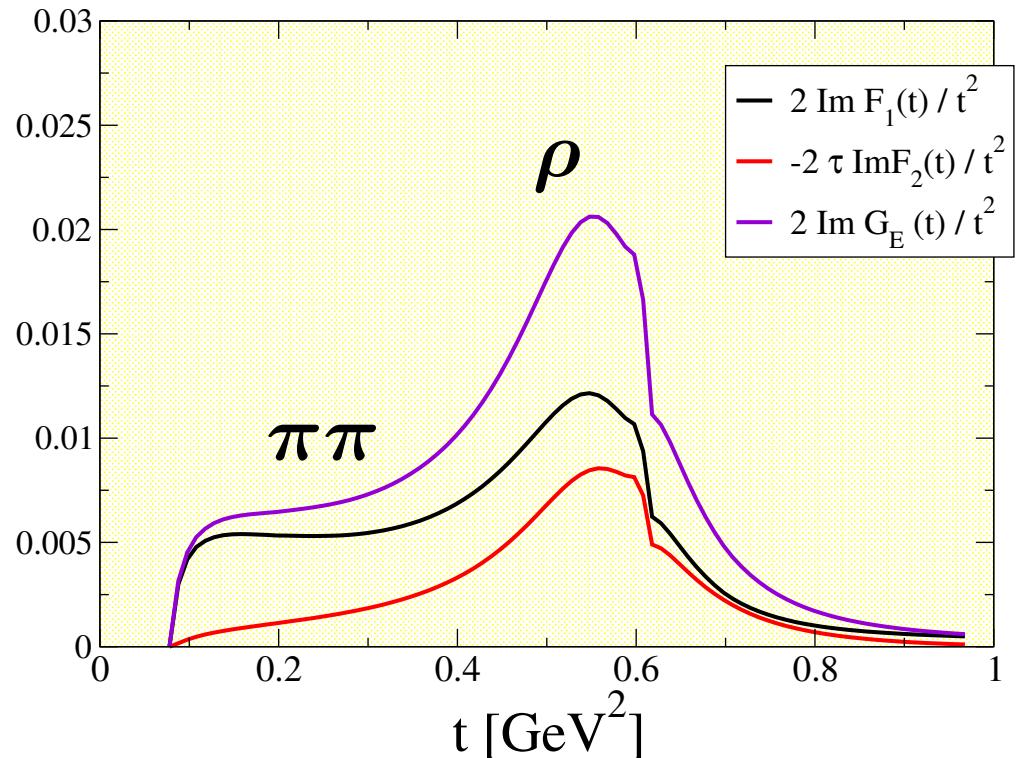
* pronounced $\rho - \omega$ mixing

KLOE Coll., Phys. Lett. B 606 (2005) 12

CMD-2 Coll., Phys. Lett. B 578 (2004) 285

SND Coll., J. Exp. Theor. Phys. 101 (2005) 1053

- Nucleon isovector spectral functions



* pronounced ρ peak

* strong shoulder on the left wing

⇒ isovector radii

ISOSCALAR SPECTRAL FUNCTIONS

- $K\bar{K}$ continuum can be extracted from analytically cont. KN scattering amplitudes
 - analytic continuation must be stabilized
 - generates most of the ϕ contribution

Hammer, Ramsey-Musolf, Phys. Rev. C **60** (1999) 045204, 045205

- Further strength in the ϕ -region generated by correlated $\pi\rho$ exchange
 - strong cancellations ($K\bar{K}$, K^*K , $\pi\rho$)
 - takes away sizeable strength from the ϕ

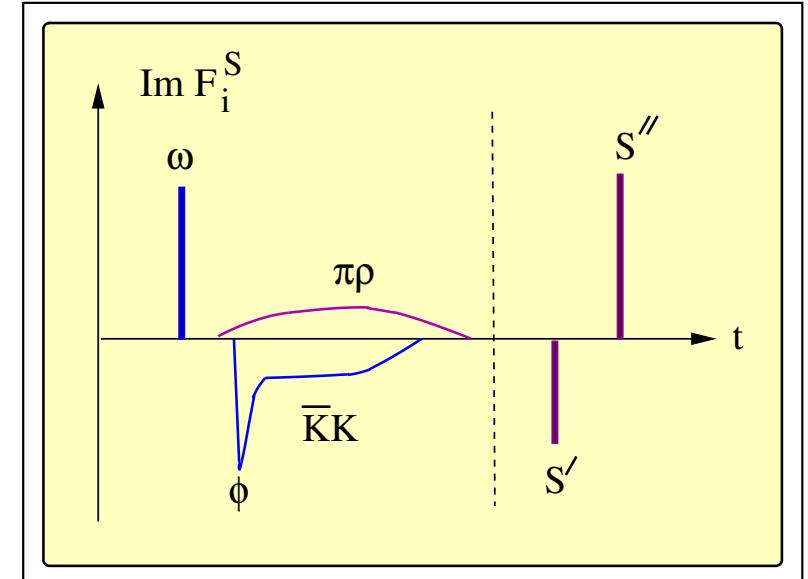
M., Mull, Speth, van Orden, Phys. Lett. B **408** (1997) 381

- Spectral functions exhibit anomalous threshold (analyzed in 2-loop CHPT)

$$t_c = M_\pi^2 \left(\sqrt{4 - M_\pi^2/m^2} + \sqrt{1 - M_\pi^2/m^2} \right)^2 \simeq 8.9 M_\pi^2 \quad \rightarrow \text{effectively masked}$$

Bernard, Kaiser, M, Nucl. Phys. A **611** (1996) 429

- Higher mass states represented by poles (with a finite width)



CONSTRAINTS ON THE SPECTRAL FUNCTIONS

- Normalizations: electric charges, magnetic moments
- Superconvergence relations \cong leading pQCD behaviour

$$F_1(t) \sim 1/t^2, F_2(t) \sim 1/t^3 \text{ (helicity - flip)}$$

Brodsky et al.

$$\Rightarrow \int_{t_0}^{\infty} \text{Im } F_1(t) dt = 0, \quad \int_{t_0}^{\infty} \text{Im } F_2(t) dt = \int_{t_0}^{\infty} \text{Im } F_2(t) t dt = 0$$

- Leading QCD logs or other α_S corrections can be included

see .e.g. Gari, Krümpelmann, Z. Phys. A **322** (1985) 689 , Mergell, M., Drechsel, Nucl. Phys. A **596** (1996) 367

⇒ severely restricts the number of fit parameters

SUMMARY: SPECTRAL & FIT FUNCTIONS

- Representation of the pole contributions: vector mesons
[NB: can be extended for finite width]

$$\text{Im } F_i^V(t) = \sum_v \pi a_i^v \delta(t - M_v^2), \quad a_i^v = \frac{M_v^2}{f_V} g_{vNN} \Rightarrow F_i(t) = \sum_v \frac{a_i^v}{M_v^2 - t}$$

- Isovector spectral functions:

$$\text{Im } F_i^V(t) = \text{Im } F_i^{(2\pi)}(t) + \sum_{v=\rho', \rho'', \dots} a_i^v \delta(t - M_v^2), \quad (i = 1, 2)$$

- Isoscalar spectral functions:

$$\text{Im } F_i^S(t) = \pi a_i^\omega \delta(t - M_\omega^2) + \text{Im } F_i^{(K\bar{K})}(t) + \text{Im } F_i^{(\pi\rho)}(t) + \sum_{v=S', S'', \dots} a_i^v \delta(t - M_v^2)$$

- Parameters: 2 for the ω , 3 (4) for each other V-mesons minus # of constraints
- Ill-posed problem → extra constraint: minimal # of poles to describe the data

Results

Belushkin, Hammer, M., Phys. Rev. **C 75** (2007) 035202 [hep-ph/0608337]

GENERAL COMMENTS ON THE FITS

- large MC sampling for initial values, successive improvement by pole reduction, new MCs, ...
- theoretical uncertainty (error bands) from $\chi^2_{\text{min}} + 1.04$ [1- σ devs.]

→ first time: dispersive analysis w/ error bars !

	this work	HM 04	recent determ.
r_E^p [fm]	0.844 (0.840...0.852)	0.848	0.880(15) [1,2,3]
r_M^p [fm]	0.854 (0.849...0.859)	0.857	0.855(35) [4]
$(r_E^n)^2$ [fm]	-0.117 (-0.11...-0.128)	-0.12	-0.115(4) [5]
r_M^n [fm]	0.862 (0.854...0.871)	0.879	0.873(11) [6]

[1] Rosenfelder, Phys. Lett. B **479** (2000) 381

[2] Sick, private communication

[3] Melnikov, van Ritbergen, Phys. Rev. Lett. **84** (2000) 1673

[4] Sick, Phys. Lett. B **576** (2003) 62

[5] Kopecky et al., Phys. Rev. C **56** (1997) 2229

[6] Kubon et al., Phys. Lett. B **524** (2002) 26

- ★ Magnetic radii in good agreement with recent determinations
- ★ Proton electric radius comes out $\lesssim 0.855$ fm

SPACE-LIKE FORM FACTORS

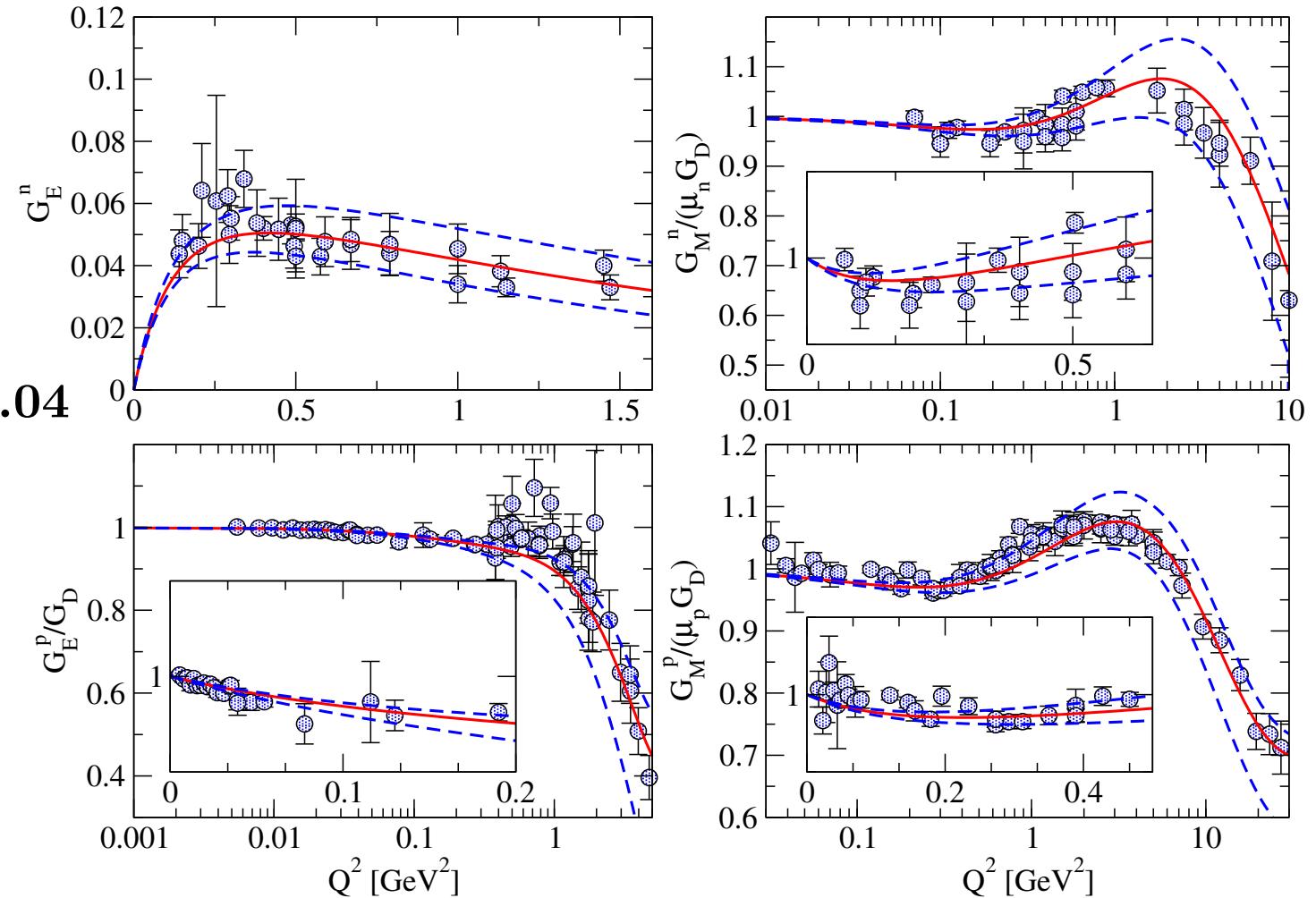
- present best fit
incl. time-like data
- 4 effective IS poles
- 4 effective IV poles
- weighted $\chi^2/\text{dof} = 1.8$
error bands: $\chi^2_{\min} + 1.04$

Improved description

- ★ JLab data described
- ★ higher mass poles
not at physical values

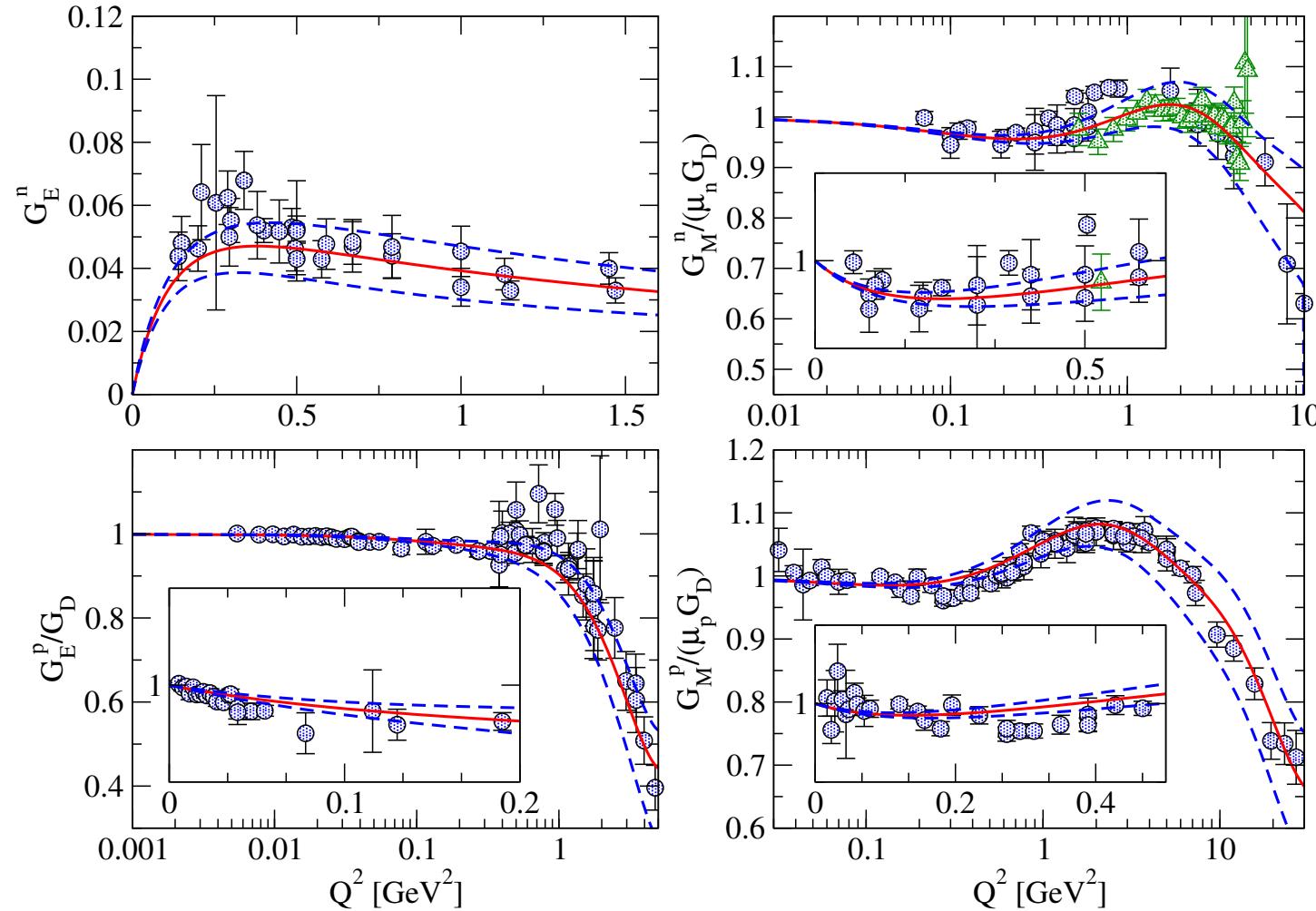
MMD 96, HMD 96, HM 04

$$G_D(Q^2) = \left(1 + \frac{Q^2}{0.71 \text{ GeV}^2}\right)^{-2}$$



SPACE-LIKE FORM FACTORS: NEW CLAS DATA

CLAS collaboration, to be published

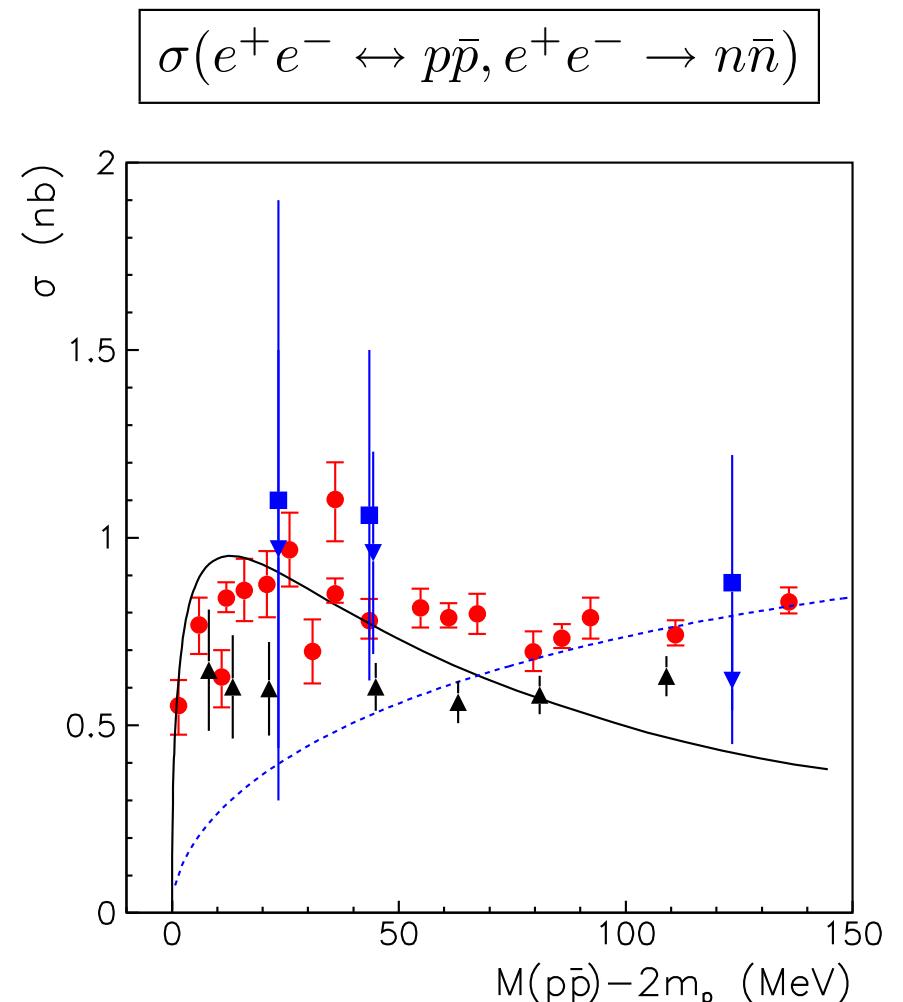


→ apparent discrepancy to be resolved

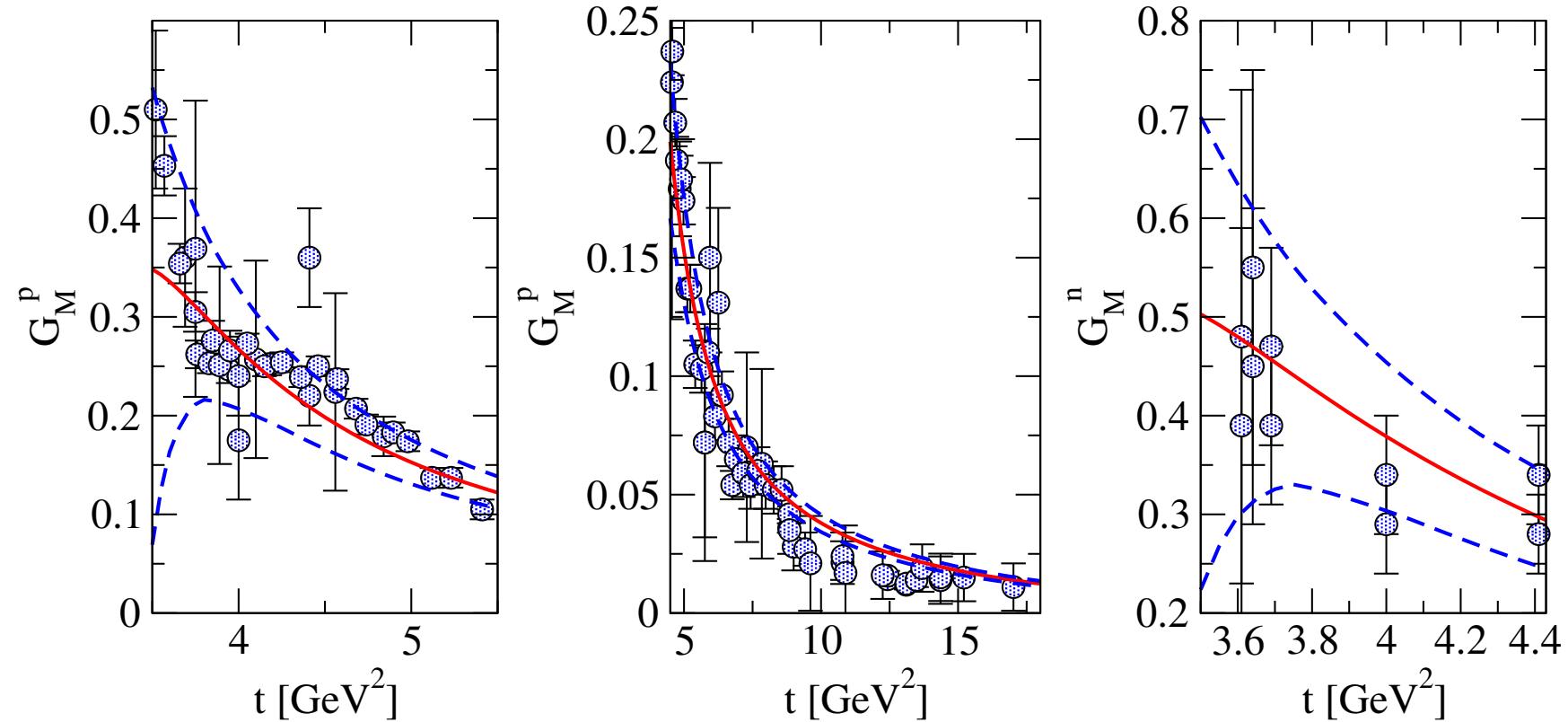
TIME-LIKE FORM FACTORS

- fitting also time-like data more complicated
- experimental extraction ambiguous
 - E/M separation
 - $\bar{N}N$ final-state interactions?
- similar to $J/\psi \rightarrow \bar{p}p\gamma$ from BES
 Sibirtsev et al., Phys. Rev. D **71** (2005) 054010
- similar to $B^+ \rightarrow \bar{p}pK^+$ from BaBar
 Haidenbauer et al., Phys. Lett. B **643** (2006) 29
- subthreshold resonance ? (or FSI ?)
 Antonelli et al., Nucl. Phys. B **517** (1998) 3
- many new proton data (radiative return)

BES, CLEO, BaBar



TIME-LIKE FORM FACTORS



- Only proton data participate in the fits
- All data within one sigma – first time consistent fit w/ space-like ffs

⇒ Need more data on time-like G_M^n

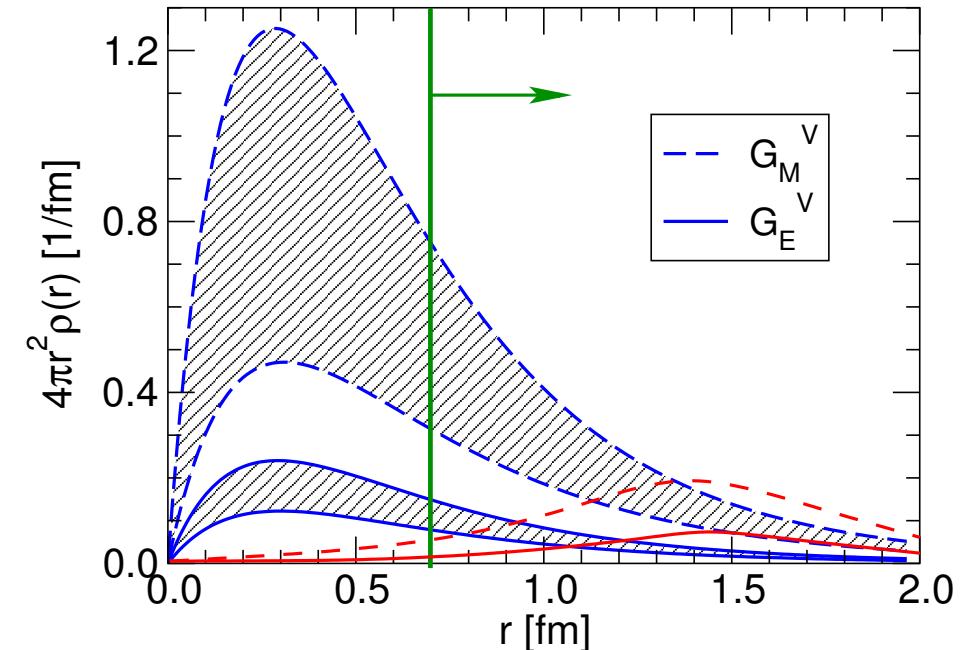
ON THE PION CLOUD OF THE NUCLEON

Hammer, M., Drechsel, Phys. Lett. B **586** (2004) 291

- FW find a very long-ranged contribution of the pion could, $r \simeq 2$ fm

Friedrich, Walcher, EPJ A **17** (2003) 607

- longest range component can be extracted from the isovector spectral function
 - separation of the ρ -contribution
 - three methods applied to do this
 - theoretical band

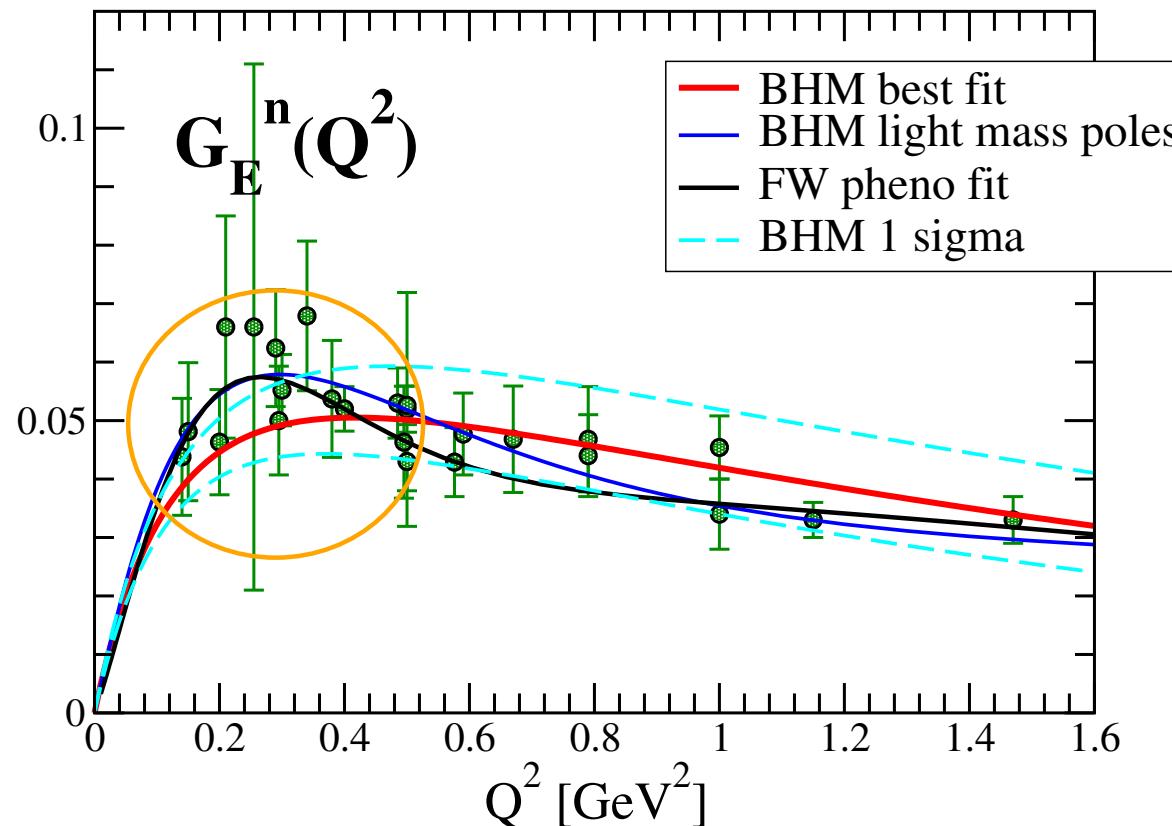


$$\rho_i^V(r) = \frac{1}{4\pi^2} \int_{4M_\pi^2}^{40M_\pi^2} dt \operatorname{Im} G_i^V(t) \frac{e^{-r\sqrt{t}}}{r} \quad (i = E, M)$$

- much smaller pion cloud contribution for $r \geq 1$ fm compared to FW
- results independent of the contributions from $t > 40M_\pi^2$

$G_E^n(Q^2)$ w/ a BUMP-DIP STRUCTURE

- can one generate a bump-dip structure in the dispersive approach?



\Rightarrow yes, but need **low-mass** poles: $M_S = 358$ MeV & $M_V = 558$ MeV

what shall these be? – not consistent w/ spec ftcs!

SUMMARY & OUTLOOK

- New dispersive analysis of the nucleon em form factors
- Improved spectral functions \Rightarrow many results
 - better fits w/ inclusion of time-like form factors
 - theoretical/systematic uncertainty \rightarrow bands
- Still to be done
 - including pQCD corrections at large- t beyond SCR
 - two-photon effects? \rightarrow fit to X sections
 - consequences for the strangeness vector form factors
 - and much more . . .